

# E-VIEW-ation – a Large-scale Evaluation Study of Association Measures for Collocation Identification

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## Abstract

Statistical association measures (AM) play an important role in the automatic extraction of collocations and multiword expressions from corpora, but many parameters governing their performance are still poorly understood. Systematic evaluation studies have produced conflicting recommendations for an optimal AM, and little attention has been paid to other parameters such as the underlying corpus, the size of the co-occurrence context, or the application of a frequency threshold.

Our paper presents the results of a large-scale evaluation study covering 13 corpora, eight context sizes, four frequency thresholds, and 20 AMs against two different gold standards of lexical collocations. While the optimal choice of an AM depends strongly on the particular gold standard used, other parameters prove much more robust: (i) small co-occurrence contexts are better than larger spans, and the best results are usually obtained from syntactic dependencies; (ii) corpus quality is more important than sheer size, but large Web corpora prove to be a valid substitute for the British National Corpus; (iii) frequency thresholds seem to be unnecessary in most situations, as the statistical AMs successfully weed out rare and unreliable candidates; (iv) there is little interaction between the choice of AM and the other parameters.

In order to provide complete evidence for our observations to readers, we created an interactive Web-based application that allows users to manipulate all evaluation parameters and dynamically updates evaluation graphs and summaries.

**Keywords:** collocations; association measures; evaluation; multiword expressions; visualization

## 1. Introduction

Traditionally, the identification of collocations and other types of lexicalized multiword expressions (MWE) has been based on co-occurrence data quantified by statistical association measures (AM). A typical extraction pipeline obtains co-occurrence counts (within a span of  $n$  words, within a sentence, or in a direct syntactic dependency relation) from a given source corpus. Candidates are then ranked according to their association scores, optionally filtered by various criteria, and finally presented to lexicographers or domain experts for manual validation (Evert, 2008).

Recent work has focused on complementing AMs with other indicators for the non-compositionality (Katz & Giesbrecht, 2006; Kiela & Clark, 2013; Yazdani et al., 2015), non-modifiability (Villada Moirón, 2005; Nissim & Zaninello, 2013; Squillante, 2014) or non-substitutability (Pearce, 2001; Farahmand & Henderson, 2016) of candidate expressions; on combining different information sources using machine learning techniques (Ramisch et al., 2010; Tsvetkov & Wintner, 2014); or on the extraction of a specific subtype of MWE (Baldwin, 2005; Tu & Roth, 2011; Smith, 2014).

Statistical association remains an important component in virtually all of these approaches, but our understanding of the properties of different AMs and of other parameters such as the size of the co-occurrence context is still incomplete. Previous evaluation studies on collocation identification (cf. Section 3) leave a number of important gaps: (i) most studies evaluate only a small range of AMs (except for Pecina, 2005); (ii) the evaluation typically focuses on a specific subtype of MWE, so that different studies often report contradictory results; (iii) to date there has been no systematic analysis of the influence of source corpus, co-occurrence context and frequency threshold.

In this paper, we present the results of a large-scale evaluation study aiming to fill these gaps. Since we believe that AMs should not be tuned to a particular subtype of MWE, but rather capture a general “attraction” between words that may then be combined with more specific indicators such as syntactic flexibility, our gold standard is based on the broad and intuitive notion of lexical collocations (see Section 2). We draw on two different English collocation dictionaries in order to assess the robustness of evaluation results. We evaluate 20 association measures, 13 corpora, eight co-occurrence contexts and four frequency thresholds against the two collocation dictionaries. In order to be able to deal with the complexity of  $20 \times 13 \times 8 \times 4 \times 2 = 16,640$  parameter combinations, we introduce an interactive Web-based viewer for evaluation graphs.<sup>1</sup>

## 2. Lexical collocations

Lexical collocations – salient co-occurrences of two lexical items (for a full definition and literature review, see Bartsch, 2004) – form a subtype of the larger family of lexicalized MWE and are notoriously difficult to delineate due to the fuzzy nature of the linguistic relation between their constituent words (which is sometimes described as a “habitual” combination, or simply defined mechanistically in terms of recurrence; e.g. Firth, 1957; Sinclair, 1966). In contrast to many other types of MWEs, lexical collocations are more susceptible to regular syntactic alternations. They are, furthermore, semantically transparent to a large degree, although many collocations carry additional, often domain-specific meanings. Examples of lexical collocations are *argue + plausibly*, *attempt + thwart* and *measure(s) + coercive*.

Our evaluation operationalizes lexical collocations as combinations of two lexical words. We assume that larger combinations such as *in a certain measure* can easily be recognized based on a two-word nucleus (*measure + certain*) by a lexicographer working with a corpus-based list of candidates, or generated by an automatic MWE extraction pipeline from the same nucleus.

Since the early days (Sinclair, 1966), the automatic identification of lexical collocations has relied primarily on the co-occurrence frequency of the words in question within a given context window. This window is typically defined as a surface span of 3 to 5 words to the left and right, but other span sizes have been employed in collocation studies ranging from one-word spans to entire sentences. Some authors define lexical collocations as a syntactic phenomenon (Bartsch, 2004), which suggests a co-occurrence context based on direct syntactic dependency relations, requiring a parsed corpus. After data extraction, researchers often apply a frequency threshold (e.g.  $f \geq 5$ ) to filter the co-occurrence data. Finally, candidates are ranked according to a statistical association measure based on the joint and marginal frequencies of each word pair; more than 50 different measures have already been proposed in the literature (Pecina, 2005).

## 3. Related work

A typical approach to assessing the quality of a collocation extraction method is to extract a ranked list of collocation candidates and to manually identify the number of true

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<sup>1</sup> Since some parameter combinations are not feasible (e.g. because a high frequency threshold does not leave enough candidates for the evaluation), the actual number of evaluation settings in our experiments and in the viewer is 12,860.

collocations among the  $n$  highest ranking candidates. This methodology is adopted, for example, by Seretan & Wehrli (2008) who compare their syntax-based extraction method with a window-based approach by manually annotating 250 candidates taken from the top 0%, 1%, 3%, 5% and 10% of the candidate lists for each of the four languages and two approaches they are looking at. Disadvantages of this evaluation methodology are that it is impossible to determine recall and that it is difficult to add new approaches or association measures to the evaluation since that would require additional manual annotation of the new candidate lists (consequently, Seretan & Wehrli, 2008 only report precision and focus on a single association measure, log-likelihood).

Another approach, introduced by Evert & Krenn (2001), focuses on a fixed set of true collocations and on the one hand allows us to determine precision and recall for arbitrarily large  $n$ -best lists of candidates and on the other hand makes it easy to add new association measures or extraction strategies to the evaluation. Results for this approach to evaluation of collocation extraction are usually given in the form of precision-recall curves. This is the approach taken, for example, by Pearce (2002) whose evaluation is based on 4,152 multiwords from the New Oxford Dictionary of English or by Pecina (2005) who evaluates a wide range of AMs based on more than 2,500 collocational dependency bigrams. Pecina & Schlesinger (2006) and Pecina (2010) also calculate the mean average precision for recall values between 0.1 and 0.9 to arrive at a single evaluation score. Kilgariff et al. (2014) do not use precision-recall curves but report precision, recall and  $F_5$ -scores (giving more weight to recall) for different combinations of parameter settings such as AM, size of the  $n$ -best candidate lists or frequency thresholds based on 5,327 collocations for 102 headwords for English and 4,854 collocations for 100 headwords for Czech.

A related approach to evaluation treats collocation extraction as a classification task and uses a test set consisting of true collocations and non-collocations, reporting the usual metrics of precision, recall and  $F$ -score. This is the approach taken, for example, by Karan et al. (2012) who evaluate machine learning models for collocation extraction for Croatian based on a test set of 84 collocations and 450 non-collocations.

Finally, there are also approaches that focus on a qualitative evaluation instead of a quantitative one. Wermter & Hahn (2006), for example, compare ranked candidate lists by looking at the true positives and true negatives in the upper and lower half of the candidate lists.

Most of these studies focus on a particular system for collocation or MWE identification, on the comparison of different AMs and the effect of linguistic filters, or on optimizing extraction quality with the help of machine learning. To our knowledge, no systematic comparative study of the influence of source corpus and co-occurrence context has been published so far.

## 4. Data and methods

### 4.1 Gold standard

We adopt the evaluation methodology of Evert & Krenn (2001) and Pecina (2005), using precision-recall graphs in order to visualize and compare the distribution of true positives in candidate lists ranked according to different AMs. As has been explained in Section 2, lexical collocations are operationalized as pairs of lexical words (nouns, verbs,

adjectives and adverbs). Since most such collocations are combinations of lexemes rather than specific word forms, all word pairs are lemmatized. We do not distinguish between homographs with different parts of speech (e.g. the noun *attempt* vs. verb *to attempt*) because one of the two sources for our gold standard does not provide POS information.<sup>2</sup>

Because of the wide scope of our study and the large number of parameter combinations to be considered, manual annotation of candidate sets extracted from the corpus – as recommended by Evert & Krenn (2001) – is not feasible. Instead, we follow Pearce (2002) in using a fixed set of known collocations as a gold standard. We obtained this gold standard from two specialized collocation dictionaries:

**BBI** = The BBI Combinatory Dictionary of English (Benson et al., 1986);

**OCD** = Oxford Collocations Dictionary for students of English, 2nd edition (McIntosh et al., 2009).

Since BBI is not available in machine-readable form, we selected a set of 203 node words based on various criteria (words sampled from different frequency bands, words known to have interesting collocational patterns, at least 4 collocates in the two dictionaries). For each of the 203 nodes, all lexical words were manually transcribed from the corresponding entries in BBI and lemmatized.

**measure I n.** 1. a cubic; dry; liquid; metric ~ 2. a tape ~ 3. in a certain ~ (in large ~) 4. (misc.) for good ~ ('as smt. extra'); made to ~ ('custom-made'); to take smb.'s ~ ('to evaluate smb.') (see also **measures**)

**measure II v.** 1. (d; tr.) to ~ against (to ~ one's accomplishments against smb. else's) 2. (P; intr.) the room ~s twenty feet by ten

**measures n.** 1. to carry out, take ~ 2. coercive; compulsory; draconian; drastic, harsh, stern, stringent; emergency; extreme, radical; preventive, prophylactic; safety, security; stopgap, temporary ~ 3. ~ to + inf. (we took ~ to insure their safety) 4. ~ against (to take ~ against smuggling)

Figure 1: BBI entries corresponding to the node lemma *measure* in our gold standard

Consider the lemma *measure* as an example. Since we do not distinguish between different POS categories, collocates are collected from three entries in the BBI dictionary (for the noun *measure*, the verb *measure* and the plural noun *measures*), as shown in Figure 1. Our annotators identified 26 lemmas of lexical words in these entries, yielding the following collocates of *measure* in the BBI gold standard: *carry, certain, coercive, compulsory, cubic, draconian, drastic, dry, emergency, extreme, good, harsh, liquid, make, metric, preventive, prophylactic, radical, safety, security, stern, stopgap, stringent, take, tape, temporary*.

The corresponding OCD collocations were extracted from an electronic version of the dictionary, using the same strategy as Uhrig & Proisl (2012). In this way, we found a total of 2,845 lexical collocations for our 203 node lemmas in the BBI, and 18,545 in the OCD. We refer to these sets as the BBI and OCD gold standard below.

<sup>2</sup> A second reason is that the Web1T5 n-gram database does not include POS tagging; application of an off-the-shelf tagger is impossible because the underlying text corpus is not publicly available.

BBI was selected in a previous study (Bartsch & Evert, 2014) as a dictionary dating from the pre-corpus age. Unlike more recent collocation dictionaries, it can safely be assumed to be free of any bias in favour of a particular corpus or collocation extraction method. There are some limitations – due to the time of its compilation, its relatively small size and scope, as well as the heterogeneity of entries<sup>3</sup> – which have to be taken into consideration when interpreting the evaluation results.

## 4.2 Corpus data and parameters

We extracted co-occurrence data from the 13 corpora listed in Table 1, ranging in size from small, relatively clean corpora such as the British National Corpus (BNC) of 100 million words to huge Web corpora of up to 16 billion words (joint Web corpus = ENCOW + WebBase + ukWaC + Wackypedia). The corpora cover a wide diversity of text types: a balanced sample (BNC), movie subtitles (DESC), newspaper data (Gigaword), encyclopaedia articles (Wackypedia), Web corpora (ukWaC, WebBase, UKCOW, ENCOW). In addition, we included n-gram databases derived from Web text (Web1T5) and scanned books (Google Books), which can also be used to obtain co-occurrence data (Evert, 2010). All corpora except for Web1T5 include POS tagging and lemmatization.

| Corpus                         | Size   |
|--------------------------------|--------|
| British National Corpus (BNC)  | 0.1 G  |
| English movie subtitles (DESC) | 0.1 G  |
| Wackypedia subset (WP500)      | 0.2 G  |
| Wackypedia (Wiki)              | 1 G    |
| ukWaC                          | 2 G    |
| Gigaword newspaper corpus      | 2 G    |
| WebBase                        | 3 G    |
| UKCOW                          | 4 G    |
| ENCOW                          | 10 G   |
| Joint Web                      | 16 G   |
| Google Books BrE               | 50 G   |
| Google Books                   | 500 G  |
| Google Web 1T5                 | 1000 G |

Table 1: Source corpora for the evaluation study. Sizes are specified in billion tokens

We extracted candidate collocations for the 203 node words using different co-occurrence contexts:

- direct syntactic relations;
- surface span of 1, 2, 3, 5 and 10 words;<sup>4</sup>
- sentence context.

We used the efficient and robust C&C parser (Clark & Curran, 2004) to extract syntactic dependencies from all corpora. For Google Books, we used the dependency bigrams

<sup>3</sup> In addition to lexical collocations proper, the BBI entries include phenomena ranging from fixed multiword units to combinations that might rather be described as colligations.

<sup>4</sup> Following Evert (2008), we denote these spans as L1/R1, L2/R2, etc. For example, a L2/R2 span includes two words to the left and two words to the right of each occurrence of the node word.

included in the database; syntactic context is not available for the Web1T5 n-grams. For surface spans, care was taken to obtain valid co-occurrence counts and marginal frequencies as mandated by Evert (2008), using the UCS toolkit.<sup>5</sup> Note that 5- and 10-word spans are not available for the Google Books and Web 1T5 n-grams. In order to keep the amount of data manageable, potential collocates were restricted to a set of 37,437 general English words.<sup>6</sup> Even so, sets of up to five million candidate pairs were obtained for the 203 node lemmas, depending on corpus and context size (cf. Table 2). Optionally, frequency thresholds were used to pre-filter the candidates.

Candidate sets were then ranked according to 20 different association measures. In addition to measures recommended by Evert (2008), we included the asymmetric  $\Delta P$  that has recently become popular in the corpus linguistics community (Gries, 2013). We evaluated the “forward”  $\Delta P_{2|1}$  and the “backward”  $\Delta P_{1|2}$  version of the measure, as well as two symmetrical variants. See Appendix A for a complete listing with equations and references.

### 4.3 Evaluation methodology

Like Evert & Krenn (2001) and Pecina (2005), we pool the candidate collocations extracted for all 203 nodes into a single set (for a given combination of corpus, co-occurrence context and frequency threshold), which is then ranked according to one of the 20 AMs. In addition, candidates are marked as true positives (TP) or false positives (FP) by comparison with either the BBI or the OCD gold standard.

After setting a cutoff threshold to obtain an n-best list of highest-ranked candidates, we compute precision ( $P$ , the percentage of TPs among the  $n$  candidates) and recall ( $R$ , the percentage of all TPs in the gold standard found in the n-best list) as quantitative evaluation criteria. The number  $n$  of candidates is chosen arbitrarily to trade off between high precision (short n-best lists) and high recall (long n-best lists). As proposed by Evert & Krenn (2001), we visualize this trade-off by plotting precision against recall for all possible  $n$ . An example can be seen in Figure 2 for the BNC corpus, syntactic context, and BBI as gold standard. Such P/R graphs allow a direct and detailed comparison of different AMs. For example, the solid blue line in Figure 2 shows that a ranking according to t-score ( $t$ ) achieves a recall of 10% of the BBI gold standard (i. e. 285 of the 2,845 BBI collocations have been found) at a precision of 20% (i. e. one in five candidates in the n-best list is a true positive). The coverage of 91.6% shown at the top of the plot is the proportion of BBI collocations found among the full set of 374,239 candidates extracted from the BNC; this coverage corresponds to the highest recall value that can be reached on this data set.

The “higher” a P/R graph is located in the plot, the better the ranking achieved by the corresponding association measure. However, sometimes P/R graphs of different measures intersect (e. g.  $\Delta P_{2|1}$  and log-likelihood  $G^2$  in Figure 2), making it difficult to determine an unambiguous ranking. A related problem of P/R graphs is that they allow a straightforward comparison of different association measures, but not of other parameters such

<sup>5</sup> <http://www.collocations.de/software.html>

<sup>6</sup> This word list comprises the lexical nodes and collocates found in BBI and OCD entries as well as all lexical words from the CUVplus dictionary (<http://ota.ox.ac.uk/headers/2469.xml>). Inflected forms were lemmatised using a heuristic mapping derived from the British National Corpus.

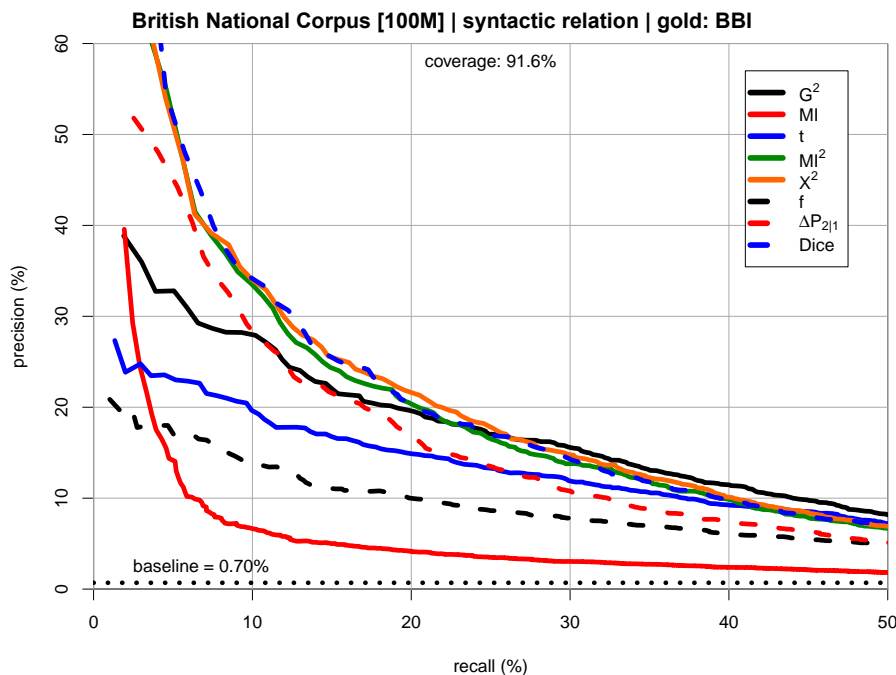


Figure 2: Precision-recall graphs for selected association measures evaluated against the BBI gold standard (British National Corpus, syntactic co-occurrence context,  $f \geq 1$ )

as source corpus and co-occurrence context (unless a single fixed association measure is chosen *a priori*).

For these reasons, it is desirable to introduce a composite evaluation criterion that summarizes the complete P/R graph into a single score. Following Pecina & Schlesinger (2006), we use average precision – corresponding to the area under a P/R graph – as a composite measure. Since recall points above 50% can only be achieved with unrealistically long n-best lists, we average precision values only up to 50% recall and refer to this composite measure as AP50.

## 5. Results

Figure 2 shows striking differences between association measures. Neither log-likelihood ( $G^2$ ), which is popular in computational linguistics, nor t-score ( $t$ ), which is popular in computational lexicography, achieve convincing performance. Mutual Information (MI) can only be described as abysmal, partly due to the lack of a frequency threshold for this data set.<sup>7</sup> The best – and almost indistinguishable – results are obtained by Pearson’s chi-squared test ( $X^2$ ), a heuristic variant of Mutual Information ( $MI^2$ ) and the Dice coefficient.<sup>8</sup> In the composite ranking of association measures,  $X^2$  takes first place with AP50 = 24.2%, followed by Dice with 24.0%. This is particularly surprising given the widely-accepted claim that  $G^2$  is vastly superior to  $X^2$  for collocation identification (Dunning, 1993).

A second striking observation is how much the evaluation results depend on which collocation dictionary is used as a gold standard, even though both are targeted at the same type

<sup>7</sup> As we will see below, frequency thresholds have little impact on the best-performing AMs, so it makes sense to present the basic findings here without a frequency threshold (i.e.  $f \geq 1$ ).

<sup>8</sup> This is particularly relevant for users of the SketchEngine (Kilgariff et al., 2004) which uses (a rescaled version of) the Dice coefficient for word sketches (Rychlý, 2008).

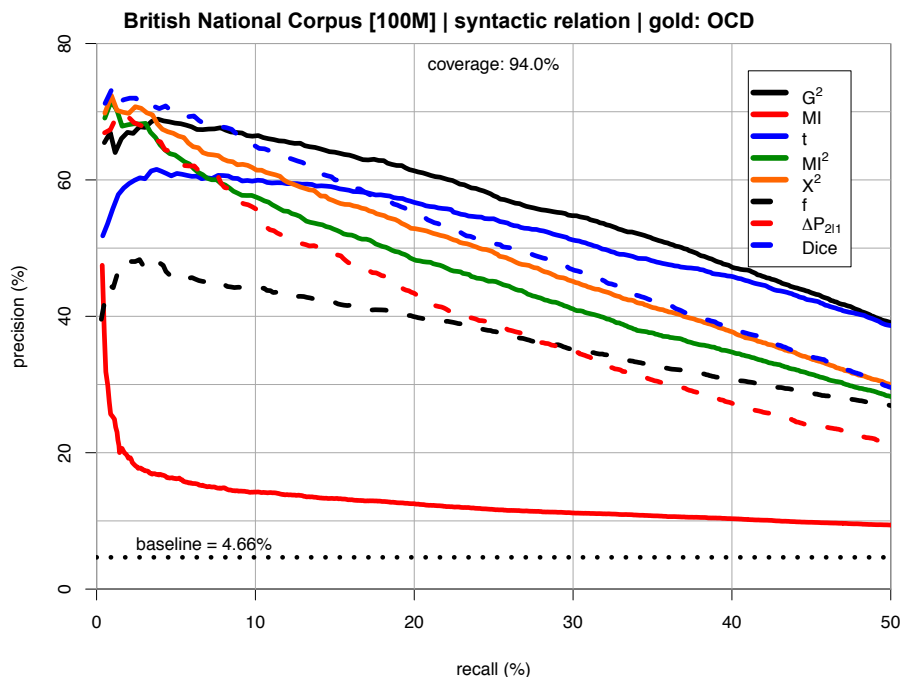


Figure 3: Precision-recall graphs for selected association measures evaluated against OCD gold standard (BNC, syntactic context,  $f \geq 1$ )

of users, i. e. foreign and second language learners. Figure 3 shows an entirely different ranking of the association measures, even though corpus and co-occurrence context are the same as in Figure 2: best results are now obtained by log-likelihood ( $G^2$ ,  $AP_{50} = 56.8\%$ ) and t-score ( $t$ ,  $AP_{50} = 52.5\%$ ).<sup>9</sup> These differences presumably reflect the more focused notion of lexical collocations underlying OCD, but also its bias towards the particular association measures used in the compilation of the dictionary.

Using  $AP_{50}$  as a composite evaluation criterion, we can now study the effects of the other parameters. For every combination of source corpus, co-occurrence context and frequency threshold, we selected the best performing association measure and used its  $AP_{50}$  value as an overall score. The left-hand panel of Figure 4 compares different co-occurrence contexts on the British National Corpus ( $f \geq 1$ ). For both gold standards, smaller contexts achieve considerably better performance, and the best results are achieved if candidate pairs must occur in a direct syntactic relation. Similar plots for other corpora and frequency thresholds (not shown for reasons of space) reveal the same pattern, except for minimal differences (e. g. L1/R1 might be slightly better than L2/R2 if a frequency threshold is applied).

The right-hand panel of Figure 4 compares results obtained on different source corpora for the same two-word co-occurrence span (which is available for all 13 corpora), again without frequency threshold ( $f \geq 1$ ). This chart shows a more intricate pattern. Summarizing, we find that:

1. Size matters: larger corpora of the same kind (WP500 vs. full Wiki; Web corpora) perform better. However, the corpus size has to be scaled up by a factor of 10 in order to achieve a notable improvement.

<sup>9</sup>  $AP_{50}$  values are also much higher overall for OCD than for BBI. This is to be expected, though, simply because of the much larger number of TPs in the OCD gold standard ( $6.5\times$  as many as in BBI).



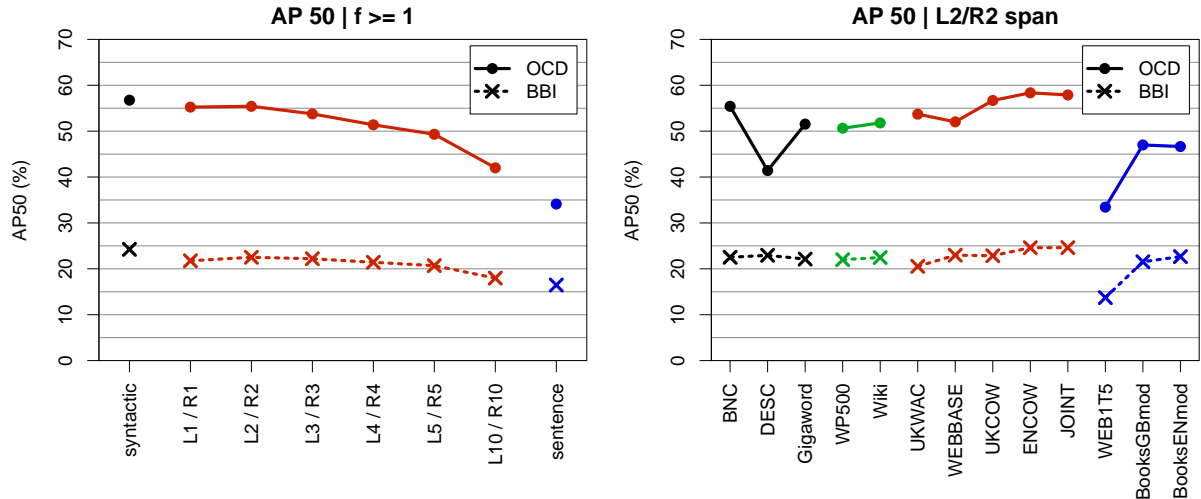


Figure 4: Left panel: Best AP50 scores achieved on the British National Corpus for different co-occurrence contexts. Right panel: Best AP50 scores achieved on different corpora with two-word co-occurrence span (L2/R2). In each case, the optimal AM has been selected

2. Clean, balanced samples (BNC) are better than large, messy Web corpora of the same size. The biggest Web corpora outperform the BNC, but this requires almost 100 times as much data (ENCOW: 10G words vs. BNC: 100M).
3. Movie subtitles (DESC), which are closer to spoken language and match psycholinguistic observations (New et al., 2007), perform better than the BNC against the BBI gold standard, but much worse when evaluated against OCD.<sup>10</sup>
4. Even though n-gram databases have been compiled from huge corpora (from 50 billion words for British GoogleBooks to 1 trillion words for Web1T5), they appear to be unsuitable for collocation identification.
5. There are some differences between the two gold standards, but the main observations hold equally well for BBI and OCD.

Again, similar plots for other co-occurrence contexts and frequency thresholds (not shown) always reveal the same pattern.

Figure 5 shows that there is virtually no interaction between the choice of AM and the other parameters (co-occurrence context and source corpus); similar patterns hold for the OCD gold standard and the other 15 AMs. The only exception is the combination of a frequency threshold with a small corpus, which improves the performance of MI (right panel). This has little practical relevance, though, because MI never comes close to the best-performing measures.

One of the most surprising results of our evaluation is the negligible impact of frequency thresholds: apparently, the statistical measures successfully weed out unreliable low-frequency candidates. Figure 6 compares a wide range of frequency thresholds on the BBI gold standard. The top panel shows that thresholds up to  $f \geq 10$  only lead to a tiny

<sup>10</sup> One possibility is that OCD in particular is focused on British English as represented in the BNC, which provided the empirical basis for the first edition of the dictionary. British films account for only 10% of the DESC corpus and the subtitle files consistently use American spelling. This would also explain the lower performance of Gigaword (mostly U.S. newspapers) and WebBase (a Web corpus compiled in the U.S., while ukWaC and UKCOW only include Web pages from .uk domains).

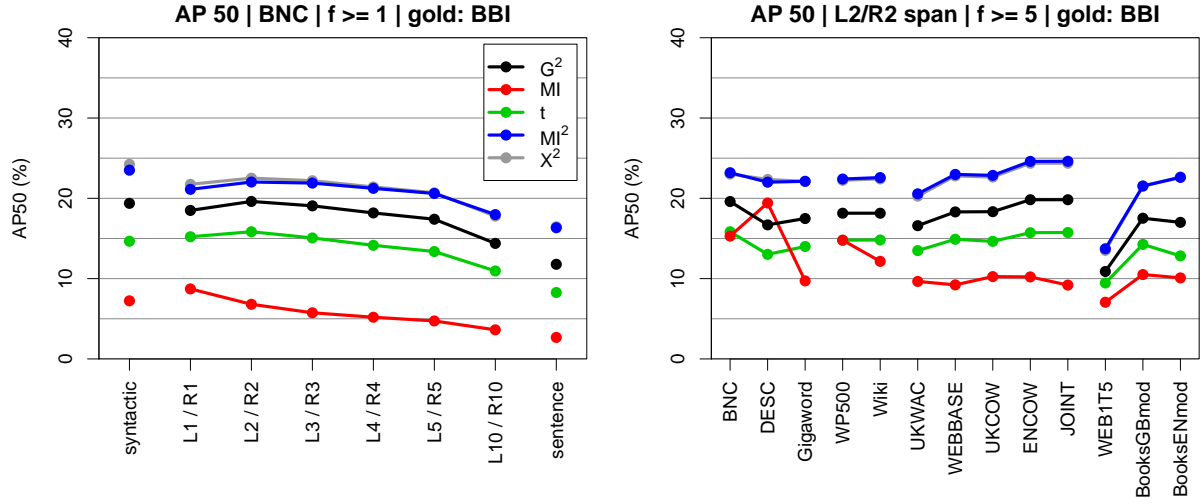


Figure 5: Co-occurrence context (left panel) and source corpus (right panel) do not interact with the choice of association measure. Illustrated for the BBI gold standard, the British National Corpus with  $f \geq 1$  (left panel) and a two-word co-occurrence span with  $f \geq 5$  (right panel)

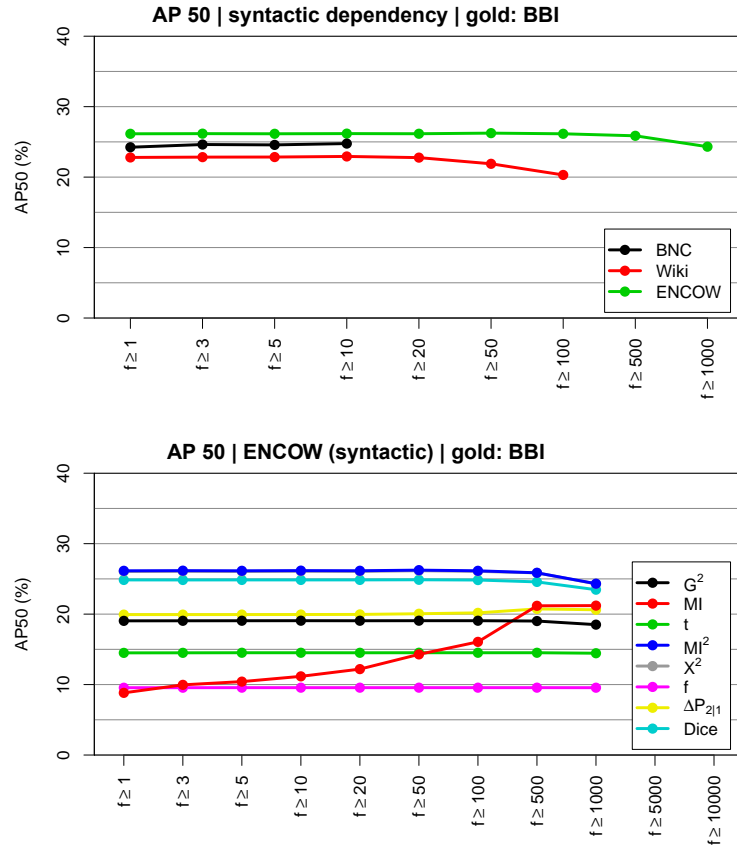


Figure 6: Effect of frequency thresholds on various corpora (top panel) and AMs (bottom panel), for syntactic context and BBI gold standard

| $f \geq 1$ |                   | BBI       |                    |               | OCD     |           |                    |             |      |
|------------|-------------------|-----------|--------------------|---------------|---------|-----------|--------------------|-------------|------|
| corpus     | $n_{\text{cand}}$ | context   | AM                 | AP50 coverage | context | AM        | AP50 coverage      |             |      |
| BNC        | 0.5M              | syntactic | $X^2$              | 24.2          | 91.6    | syntactic | $G^2$              | 56.8        | 94.0 |
| DESC       | 0.3M              | syntactic | $MI_{\text{conf}}$ | 24.6          | 80.9    | syntactic | $MI_{\text{conf}}$ | 44.0        | 72.8 |
| Gigaword   | 1.2M              | L2/R2     | $X^2$              | 22.1          | 97.6    | L1/R1     | $G^2$              | 52.3        | 95.6 |
| WP500      | 0.5M              | syntactic | $X^2$              | 22.6          | 92.2    | L2/R2     | $G^2$              | 50.6        | 92.8 |
| Wiki       | 1.0M              | syntactic | $MI^2$             | 22.8          | 97.0    | L2/R2     | $G^2$              | 51.8        | 97.4 |
| ukWaC      | 1.4M              | syntactic | $MI^2$             | 22.8          | 98.7    | L1/R1     | $G^2$              | 56.5        | 97.5 |
| WebBase    | 1.7M              | syntactic | $MI^2$             | 25.1          | 99.2    | syntactic | $G^2$              | 54.2        | 99.5 |
| UKCOW      | 1.9M              | syntactic | $MI^2$             | 24.6          | 99.3    | L1/R1     | $G^2$              | 58.0        | 98.1 |
| ENCOW      | 2.5M              | syntactic | $MI^2$             | 26.1          | 99.7    | L1/R1     | $G^2$              | <b>59.7</b> | 98.7 |
| Joint      | 2.8M              | syntactic | $MI^2$             | <b>26.4</b>   | 99.8    | L1/R1     | $G^2$              | 59.5        | 99.4 |
| Web1T5     | 1.8M              | L1/R1     | $MI^2$             | 15.5          | 97.5    | L1/R1     | $MI^3$             | 37.1        | 97.9 |
| BooksGB    | 0.9M              | syntactic | $MI^2$             | 21.7          | 95.4    | L1/R1     | $G^2$              | 47.9        | 93.0 |
| BooksEN    | 1.5M              | syntactic | $MI^2$             | 22.8          | 96.1    | syntactic | $G^2$              | 48.6        | 96.9 |

Table 2: Overview table of best evaluation result for each corpus against the BBI and OCD gold standard (coverage indicates the highest recall point that can be achieved by a given parameter combination)

improvement for the smallest corpus (BNC) and have no effect at all for larger corpora. The bottom panel shows that thresholds mainly help to counteract the low-frequency bias of the MI measure. All other AMs are unaffected, and even with a high threshold, MI remains well below the best-performing measures.

A detailed overview of the evaluation results is shown in Table 2. For each source corpus, the AP50 score achieved by the optimal co-occurrence context and association measure is shown, as well as the coverage of the respective gold standard. In order to indicate the amount of data processed, the second column ( $n_{\text{cand}}$ ) shows how many million word pairs were extracted from each corpus for a two-word surface span (L2/R2).

## 6. An interactive viewer

Any paper-length treatment of association measures is faced with the problem that the large number of parameter settings makes it impossible to give the reader a full overview of their influence in all possible combinations. For example, in Section 5 we showed the influence of source corpus and co-occurrence context based on AP50 values achieved by the best AM in each case. Such summary charts hide important details of the trade-off between precision and recall (e.g. some applications may prefer a measure that achieves very high precision even if recall is only 10%); they also cannot show whether the overall shape of a P/R graph remains stable across different parameter settings. Even so, space constraints make it impossible to provide comprehensive evidence for all our observations within this paper (e.g. the similar effect of parameters for both gold standards, and in particular the consistently small impact of frequency thresholds). Figures 2, 3 and 5 can only show a small selection of the 20 association measures included in our evaluation. While correlations between the rankings for different association measures (Figure 7) provide an objective criterion for a principled selection – each group of almost perfectly correlated measures (Dice and Jaccard; chi-squared and z-score; MI, relative risk and two variants of the odds ratio) can be represented by one member – there are only few such strong correlations. Moreover, even measures with correlation  $\rho > .99$  (e.g. log-likelihood,

t-score and chi-squared) sometimes achieve substantially different results in the evaluation (cf. Figures 2 and 3) and should not be grouped together.<sup>11</sup>

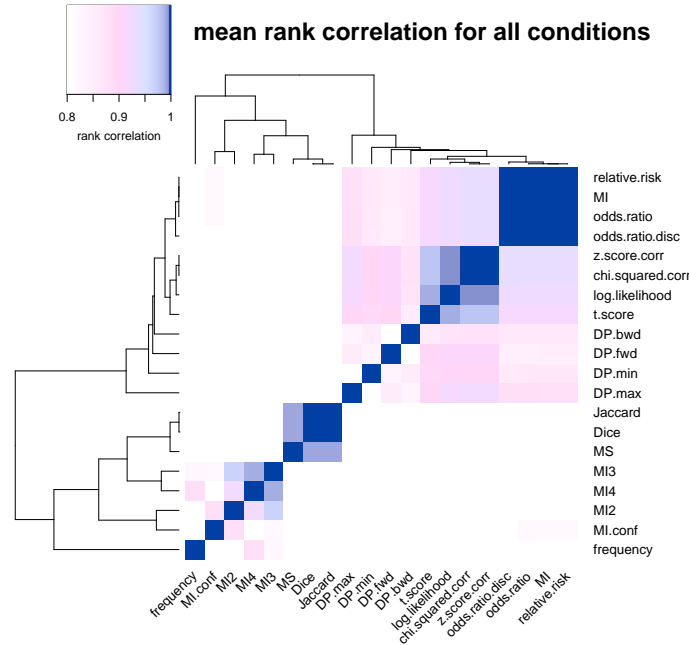


Figure 7: Spearman rank correlation of different association measures, averaged over all experimental conditions

In order to remedy these problems, an interactive viewer was created to complement the present paper and allow the reader to explore the influence of the parameters discussed above as well as their interactions.

Since the extraction of collocations candidates from large corpora is a very time-consuming process,<sup>12</sup> all evaluation graphs have been pre-computed using the statistical software R and exported as a set of JSON files. These files are processed further, filtered and served through a REST API with the help of Perl scripts. The front-end of the viewer is written in JavaScript and provides a set of sliders and buttons to modify the following parameters:

1. gold standard (BBI vs. OCD2);
2. corpus (see Section 4);
3. co-occurrence context (syntactic relation, various spans, whole sentence);
4. frequency threshold ( $f \geq 1, 5, 50, 1000$ );<sup>13</sup>
5. association measures (select measures to be displayed at the same time).

<sup>11</sup> We believe that this surprising observation is connected to the fact that rank correlations were computed over very large data sets comprising a million candidate pairs and more. Crucial differences between the rankings of the relatively small number of TPs, which affect the evaluation scores directly, are lost among the rankings of many irrelevant FPs. This example shows clearly how difficult and counter-intuitive the interpretation of correlation coefficients can be.

<sup>12</sup> The extraction procedure ran for several weeks on a high-end server (16 cores and 256 GiB RAM).

<sup>13</sup> Since the sizes of the corpora used in this study vary by several orders of magnitude, the range of thresholds is quite wide. Keep in mind that a threshold of  $f \geq 5$  in the BNC (100M words) corresponds to a threshold of  $f \geq 500$  in UKCOW (10G words). It might be profitable to explore thresholds relative to corpus size in future work.

The full P/R graphs for the chosen parameter settings are displayed to the user and dynamically updated as the sliders are moved. Additionally, coverage and composite AP50 scores are shown. The viewer software will be made available under an open-source license, including the R code for exporting suitable JSON data. An online version for the evaluation reported here can be accessed at <http://www.collocations.de/evaluation/>.

## 7. Conclusion

The systematic evaluation of different association measures, source corpora, co-occurrence contexts and frequency thresholds in a collocation extraction tasks fills important gaps in the current state of research into AMs and MWE identification.

We were able to show that the carefully sampled British National Corpus is superior to comparably-sized messy Web corpora for the identification of lexical collocations. However, sufficiently large Web corpora (close to 10 billion words) achieve similarly good or even better results than the BNC. Concerning the co-occurrence context, it was shown that small spans deliver more accurate information than larger contexts and the most restricted context, i. e. syntactic dependency, is almost always the best choice. Contrary to widespread assumptions, frequency thresholds have very little effect except to counteract the low-frequency bias of the MI measure.

The choice of an optimal AM is a more intricate problem, which depends not only on the type of MWE to be identified (lexical collocations in our case) but also on the specific definition of this MWE type, embodied by the two different collocation dictionaries (BBI and OCD) in our study. For BBI, Pearson's chi-squared statistic ( $X^2$ ) and  $MI^2$  yield the best results; for OCD, log-likelihood ( $G^2$ ) is the optimal AM. Fortunately, performance differences between AMs do not interact with the other parameters: in all cases, very large Web corpora and small co-occurrence contexts produce the best results. It is thus valid to optimize AMs independently of these parameters in future research.

Since the present evaluation builds entirely on English data, no conclusions regarding other languages can be drawn and further research is required. Nonetheless, it is to be expected that collocation extraction for languages with a richer morphology and/or a freer word order, e. g. German or Russian, will benefit from larger window sizes and in particular from dependency parsing. This would be in line with the results by Ivanova et al. (2008) and Ambati et al. (2012).

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## A. Association measures

The listing below details the complete list of statistical association measures included in our evaluation. Equations are specified using the notation of Evert (2008):



| expected frequencies |                              |                              | observed frequencies |           |                  |
|----------------------|------------------------------|------------------------------|----------------------|-----------|------------------|
|                      | collocate                    | $\neg$ collocate             |                      | collocate | $\neg$ collocate |
| node                 | $E_{11} = \frac{R_1 C_1}{N}$ | $E_{12} = \frac{R_1 C_2}{N}$ | node                 | $O_{11}$  | $O_{12} = R_1$   |
| $\neg$ node          | $E_{21} = \frac{R_2 C_1}{N}$ | $E_{22} = \frac{R_2 C_2}{N}$ | $\neg$ node          | $O_{21}$  | $O_{22} = R_2$   |
|                      |                              |                              | $= C_1$              | $= C_2$   | $= N$            |

$O_{ij}$  = contingency table of observed frequencies

$O_{11}$  = observed co-occurrence frequency

$E_{ij}$  = contingency table of expected frequencies

$E_{11}$  = expected co-occurrence frequency

$R_i$  = row sums of the contingency table

$R_1$  = marginal frequency of node

$C_j$  = column sums of the contingency table

$C_1$  = marginal frequency of collocate

$N$  = sample size

- **log-likelihood** (Dunning, 1993)

$$G^2 = 2 \sum_{ij} O_{ij} \log \frac{O_{ij}}{E_{ij}}$$

- **chi-squared** test (with Yates's correction)

$$X^2 = \frac{N \left( |O_{11}O_{22} - O_{12}O_{21}| - \frac{N}{2} \right)^2}{R_1 R_2 C_1 C_2}$$

- **t-score** (Church et al., 1991)

$$t = \frac{O_{11} - E_{11}}{\sqrt{O_{11}}}$$

- **z-score** (with Yates's (1934) correction)

$$z = \frac{O_{11} - E_{11} \pm \frac{1}{2}}{\sqrt{E_{11}}}$$

- **co-occurrence frequency**

$$f = O_{11}$$

- **mutual information** (Church & Hanks, 1990)

$$\text{MI} = \log_2 \frac{O_{11}}{E_{11}}$$

- **MI<sup>k</sup>** (Daille, 1994)

$$M^k = \log_2 \frac{(O_{11})^k}{E_{11}} \quad \text{for } k = 2, 3, 4$$

- **conservative MI** (Johnson, 1999)

$$\text{MI}_{\text{conf}, \alpha} = \log_2 \min$$

$$\left\{ \mu > 0 \mid e^{-\mu E_{11}} \sum_{k=O_{11}}^{\infty} \frac{(\mu E_{11})^k}{k!} \geq 10^{-5} \right\}$$

- **Dice** coefficient

$$\text{Dice} = \frac{2O_{11}}{R_1 + C_1}$$

- **Jaccard** coefficient

$$\text{Jaccard} = \frac{O_{11}}{O_{11} + O_{12} + O_{21}}$$

- **minimum sensitivity** (Pedersen & Bruce, 1996)

$$\text{MS} = \min \left\{ \frac{O_{11}}{R_1}, \frac{O_{11}}{C_1} \right\}$$

- **log odds ratio** (with optional discounting)

$$\begin{aligned} \log \theta &= \log \frac{O_{11}O_{22}}{O_{12}O_{21}} \\ \log \theta_{\text{disc}} &= \log \frac{(O_{11} + \frac{1}{2})(O_{22} + \frac{1}{2})}{(O_{12} + \frac{1}{2})(O_{21} + \frac{1}{2})} \end{aligned}$$

- **log relative risk**

$$r = \log \frac{O_{11}C_2}{O_{12}C_1}$$

- forward or backward **Delta P** (Gries, 2013)

$$\begin{aligned} \Delta P_{2|1} &= \frac{O_{11}}{R_1} - \frac{O_{21}}{R_2} \\ \Delta P_{1|2} &= \frac{O_{11}}{C_1} - \frac{O_{12}}{C_2} \end{aligned}$$

- **symmetrical Delta P**

$$\begin{aligned} \Delta P_{\min} &= \min \left\{ \Delta P_{2|1}, \Delta P_{1|2} \right\} \\ \Delta P_{\max} &= \max \left\{ \Delta P_{2|1}, \Delta P_{1|2} \right\} \end{aligned}$$

## B. Set of node lemmas

The following 203 lemmas were used as node words in our evaluation experiments: *abortion, accountant, achievement, act, advantage, affair, allocation, amusement, appetite, argue, art, artery, assault, attempt, authority, back, bag, balance, ban, basket, battery, battle, beach, bean, beat, beef, beg, bend, bent, biology, blast, bomb, bone, boot, break, broth, brother, bulb, bulletin, burst, cancer, carbon, care, cell, chain, chance, change, character, check, chess, chief, child, citizen, claim, clean, cleaner, cliff, close, cold, collaboration, commitment, confinement, consequence, cooking, cord, cotton, crime, criminal, cry, cupboard, cut, decision, deny, diet, director, door, draft, dressing, drunk, earth, elbow, enforce, environment, error, examination, executive, fee, feedback, fellowship, fever, fin, finger, fist, fitness, flow, fly, force, forgive, foundation, fund, funeral, garlic, gas, gender, gene, get, go, goal, gown, harm, havoc, head, health, heater, heating, heaven, heed, hernia, high, hotel, humanity, hygiene, injury, inmate, insight, intercourse, jam, juice, kick, know, lapse, letter, light, line, majority, malice, maniac, measure, measurement, meat, mechanic, membrane, minister, mother, move, nail, negligence, open, paint, pan, pardon, pay, pie, pipe, place, plague, plant, plantation, plead, pool, power, prime, problem, progress, query, question, quilt, race, radio, range, remark, representation, resuscitation, right, sauce, say, sentence, set, shake, shotgun, shoulder, soda, spirit, state, steel, storm, syllable, take, thirst, time, toss, trample, trial, triangle, tune, ulcer, universal, vacuum, vein, way, weapon, wiper, wire*

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